

Power of a Function/Chain Rule for Derivatives

Find the derivatives for each of the following functions and express in factored form:

1. $(2x - 1)^2(3x + 4)^2$

2. $(x^2 + 1)^2(x^3 + 8)$

3. $(x^2 + x)^2(2x + 5)^2$

4. $(3x + 2)^3(5 - x^2)$

5. $(2 + x)^{-1}(x^2 + 4)$

6. $(x - 1)^{-2}(x + 4)$

7. $(2x - 1)^{-1}(x + 2)^{-2}$

8. $x\sqrt{1 - x^2}$

9. $(x + 3)\sqrt{x^2 + 2x}$

10. $(3x + 1)\sqrt{x^2 - 5}$

11. $(3 - 5t)\sqrt{1 - 3t^2}$

12. $(5t - 3)\sqrt{3t^2 - 2t}$

13. $(3 - t)\sqrt{5t^2 + 3t + 1}$

14. $(x^2 + 3x)\sqrt{3x + 5}$

15. $\sqrt{1 - 3x}\sqrt{3x^2 - 5}$

16. $\sqrt{1 + x^3}\sqrt{1 - x^2}$

17. $\sqrt{x^2 - 3x}\sqrt{x^3 - 5}$

18. $\sqrt[3]{3x + x^3}\sqrt{x^2 - 2}$

Answers

1. $2(2x - 1)(3x + 4)(12x + 5)$

2. $x(x^2 + 1)(7x^3 + 3x + 32)$

3. $2x(x + 1)(2x + 5)(6x^2 + 14x + 5)$

4. $(3x + 2)^2(45 - 4x - 15x^2)$

5. $(x^2 + 4x - 4)(x + 2)^{-2}$

6. $-(x - 1)^{-3}(x + 9)$

7. $-2(3x + 1)(2x - 1)^{-2}(x + 2)^{-3}$

8. $(1 - x^2)^{-\frac{1}{2}}(1 - 2x^2)$

9. $(x^2 + 2x)^{-\frac{1}{2}}(2x^2 + 6x + 3)$

10. $(x^2 - 5)^{-\frac{1}{2}}(6x^2 + x - 15)$

11. $(1 - 3t^2)^{-\frac{1}{2}}(30t^2 - 9t - 5)$

12. $3(3t^2 - 2t)^{-\frac{1}{2}}(10t^2 - 8t + 1)$

13. $-\frac{1}{2}(5t^2 + 3t + 1)^{-\frac{1}{2}}(20t^2 - 21t - 7)$

14. $\frac{1}{2}(3x + 5)^{-\frac{1}{2}}(15x^2 + 47x + 30)$

15. $-\frac{3}{2}(1 - 3x)^{-\frac{1}{2}}(3x^2 - 5)^{-\frac{1}{2}}(9x^2 - 2x - 5)$

16. $-\frac{1}{2}x(1 - x^2)^{-\frac{1}{2}}(1 + x^3)^{-\frac{1}{2}}(5x^3 - 3x + 2)$

17. $\frac{1}{2}(x^3 - 5)^{-\frac{1}{2}}(x^2 - 3x)^{-\frac{1}{2}}(5x^4 - 12x^3 - 10x + 15)$

18. $(x^2 - 2)^{-\frac{1}{2}}(3x + x^3)^{-\frac{2}{3}}(2x^4 + 2x^2 - 2)$